

- NB:** 1) Question no.1 is compulsory.
 2) Attempt any three from remaining five questions.
 3) Assume suitable data if required.

- Q.1 a)** Explain Truncation error with suitable example. **5**
b) Explain working rule for bisection method. **5**
c) Evaluate $\int_0^6 \frac{dx}{1+x^2}$ **5**
 by applying i) Trapezoidal rule ii) Simpson's 1/3 Rule
d) Fit a straight line using the following Time Vs Conversion data. **5**

T	3	5	7	9	11
CA	2.3	2.6	2.8	3.2	3.5

- Q.2 a)** Find the approximate root of $x \log_{10} x - 1.2 = 0$ by false position method. **10**
b) Calculate the volume of superheated steam at 100 atm and 350°C using equation. **10**

$$\left(P + \frac{a}{V^2}\right)(V - b) = RT$$

Using Newton Raphson method. For initial values of V use ideal gas equation.

Where $a = \frac{27R^2T_c^2}{64P_c}$ and $b = \frac{RT_c}{8P_c}$

$T_c = 647.11$ K,

$P_c = 220.76$ atm,

$R = 8.206 \times 10^{-5}$ atm /mol. K

- Q.3 a)** Solve the following system of equations by Gauss-Jordan method. **10**

$$x + y + z = 3$$

$$x + 4y + 9z = 6$$

$$x + 2y + 3z = 4$$

- b)** The spherical storage tank containing oil has a diameter of 6 ft. Calculate the height h to which a dipstick 8 ft long would be wet with oil when immersed in the tank when it contains 4 ft³ of oil. The equation that gives the height, h, of the liquid in the spherical tank for the given volume and radius is given by $V = \frac{3\pi h^2(3r-h)}{9}$, Use the Bisection Method to find the height (h), to which the dipstick is wet with oil. **10**

Q.4 a) A dynamic model for flow through cylindrical tank is given by: **10**

$$\frac{dh}{dt} = \frac{F_o - F}{\pi D^2/4}$$

Where, D=diameter of tank; h= level in tank,
Fo =inlet flowrate; F=outlet flowrate

If tank dimensions are as given below; find the liquid level in the tank; with respect to time. Take step-size of h= 5sec; and show calculations till 20seconds. Using Runge Kutta order 2 method.

Data given:

Diameter of tank= 1m

Height of tank= 2m

F= 0.04√h in m³/s where h is in meter.

Fo =0.06 m³/s

At t=0 seconds, h=1.0 m

b) A chemical reaction is carried out in a batch reactor and the changes in concentration of reactants is given by **10**

$$\frac{dC_A}{dt} = \frac{C_A}{0.6 + 2 C_A}$$

Initially at t=0, C_A= 1. Find C_A at t=1 using Runge- Kutta second order method with h=0.5.

Q.5 a) An insulated metal rod has an initial temperature profile given by table below, find change in **10**

Length (x)	1.0	1.2	1.4	1.6	1.8	2.0	2.2
Temperature(y)	2.7183	3.3201	4.0552	4.9530	6.0496	7.3891	9.0250

temperature ($\frac{dy}{dx}$) at length 1.2 m, using Newton's Forward Difference method.

b) Solve by Crank-Nicholson method for the equation $u_{xx} = u_t$ subject to $u(x,0) = 0$, $u(0,t) = 0$ and $u(1,t) = t$ for two-time steps. **10**

Q.6 a) Use Bender- Schmidt method to solve **10**

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$$

For $u = \sin(\pi x)$ for $t=0$ where $0 < x < 1$,

$u=0$ for $x=0$ and $x=1$ for $t=0$ to 0.06 and increment in t is $k=0.02$ and in x is $h=0.2$.

Evaluate the value of u for $t = 0$ to 0.06 and $x=0$ to 1.

b) Using Crank Nicholson method solve the equation $u_{xx} = 16 u_t$, $0 < x < 1$, $t > 0$ Given $u(x,0) = 0$, $u(0,t)=0$, $u(1,t) = 100t$. Compute u for one step in t direction taking $h = \frac{1}{4}$. **10**
