12/12/2018 1T01125 - T.E.(ELECTRONICS)(Sem V)(Choice Based) / 32306 - Elective I: Digital Control System

(3 hours) [Total Marks: 80]

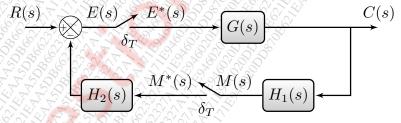
Note:

- 1. Question-1 is compulsory.
- 2. Answer any three questions from remaining five.
- 3. Assume suitable data if necessary.
- 4. Numbers in the right indicate marks.
- 1. Answer the following questions. (Each question carry 5 marks)

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- (a) Describe the data holding in digital systems and derive the transfer function of zero-order hold (ZOH).
- (b) Draw the frequency spectrum of the ideal low-pass filter and comment on its realizability with justification.
- (c) Explain quantization in digital control systems and derive the bound on the quantization error.
- (d) Clearly explain the distinction between detectability and observability for discrete-time systems.
- 2. (a) Describe bilinear transformation approach for discretization of continuoustime systems in detail. Also, comment on the mapping between s-plane and z-plane under such discretization.
 - (b) Discretize continuous-time PID controller using trapezoidal rule to approximate integral term and two-point difference to approximate derivative term.
- 3. (a) Derive the closed-loop pulse transfer function $\frac{C(s)}{R(s)}$ for the digital control system shown in figure below. Assume sampling time to be 1 second.



(b) Make a rough sketch of root locus of a unity feedback digital control system 10 whose open loop transfer function is given as

$$G(z) = \frac{Kz(1 - e^T)}{(z - 1)(z - e^T)}$$

Also determine the critical value of K. Take sampling frequency $f_s = 1$ Hz.

4. (a) Design the state feedback controller $u[k] = Kx[k] + k_0r[k]$ such that the steady-state error of the closed loop is zero for the unit step input.

$$x[k+1] = \begin{bmatrix} -0.6 & 0 & 0 \\ 0 & 0.3 & 0 \\ 0 & 0 & -0.8 \end{bmatrix} x[k] + \begin{bmatrix} 2 \\ 0.6 \\ 1 \end{bmatrix} u[k]$$

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- (b) Represent the discrete-time system of Q-4(a) in controllable canonical form and observable canonical form using similarity transforms.
 - 10
- **5**. (a) Discretize the continuous time state-space equation $\dot{x} = Ax + Bu$ and obtain the discrete-time state-space representation.
- 10
- (b) Design a deadbeat controller for the following discrete-time system.
- 10

$$x[k+1] = \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix} x[k] + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u[k]$$

6. Answer any three of the following questions: 20

- (a) Derive the mapping between s-plane and z-plane when discretizing a continuous-time system using impulse invariance approach. Determine the region of stability on z-plane under this mapping.
- (b) Determine the stability of a discrete-time system which has characteristic equation $z^4 + 1 = 0$.
- (c) Explain the distinction between observability and detectability.

