Q.P. Code: 37610

Duration: 3 hours

N. B.: 1. Question No. 1 is Compulsory.

- 2. Attempt any 3 Questions from Question no. 2 to 6.
- 3. Figures to the right indicate the full Marks.
- 4. Statistical tables are allowed.



- Que. 1 a If λ is an eigen value of nonsingular matrix A then prove that $\frac{|A|}{\lambda}$ is an eigen value of adj A.
 - b If the random variable X takes the values 1, 2, 3, 4 such that 2P(X=1)=3P(X=2)=P(X=3)=5P(X=4), find the probability distribution and cumulative distribution of X.
 - Find a basis for the orthogonal complement of the subspace in R^3 spanned by the vectors $V_1 = (1, -1, 3)$, $V_2 = (5, -4, -4)$, $V_3 = (7, -6, 2)$.
 - d Evaluate the complex line Integral $\oint_C \log z \, dz$ where C is the unit circle 5
- Que.2. a If $A = \begin{bmatrix} 2 & 3 & 4 \\ 0 & 4 & 2 \\ 0 & 0 & 3 \end{bmatrix}$ find eigen values and eigen vectors of A^2 -2A+I.
 - b Seven dice are thrown 729 times. How many times do you expect at least 4 dice to show 3 or 5?
 - Find all Taylor and Laurent series expansions for $f(z) = \frac{z}{(z-3)(z-4)}$ 8 about z=1 indicating the region of convergence.
- Que.3. a A box contains 2^n tickets, among which nC_i tickets bear the number i; i=0,1,2,...n. A group of m tickets are drawn. What is the expectation of their numbers.
 - b Verify Cayley-Hamilton theorem for $A = \begin{bmatrix} 3 & 2 & -1 \\ 0 & 2 & 0 \\ 1 & 1 & 2 \end{bmatrix}$ and hence find 6
 - c Obtain the equations of the lines of regression for the following data. Also obtain the estimate of X for Y=70.

X	65	66	6/	6/	68	69	70	/2
Y	67	68	65	68	72	72	69	71

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- Que.4. a Evaluate $\oint_C \frac{z-1}{(z+1)^2(z-2)} dz$ where C is |z| = 3
 - b Construct an orthonormal basis of R^3 using Gram Schmidt process to $S=\{(3,0,4),(-1,0,7),(2,9,11)\}$
 - Determine whether the matrix $A = \begin{bmatrix} 8 & -8 & -2 \\ 4 & -3 & -2 \\ 3 & -4 & 1 \end{bmatrix}$ is diagonalizable, if yes diagonalise it.
- Que. 5 a Show that the matrix $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$ is derogatory and find the minimal polynomial of the matrix.
 - b A random variable X has probability density function $\frac{1}{2^x}$, x=1,2,3,.. Find moment generating function and hence find mean and variance of X.
 - c Of a group of men 5% are under 60 inches height and 40% are between 8 60 and 65 inches. Assuming a normal distribution find the mean height and standard deviation.

Que.6. a If
$$A = \frac{1}{2} \begin{bmatrix} 3 & 1 \\ 1 & 3 \end{bmatrix}$$
 find e^A and 4^A

- b Between 2 pm and 4 pm, the average number of phone calls per minute coming into a switchboard of a company is 2.5. Find the probability that during one particular minute there will be (i) no phone call at all, (ii) at least 5 calls.
- c By using Cauchy residue theorem, evaluate

$$\int_{0}^{\infty} \frac{dx}{x^2 + 4}$$
 ii.
$$\int_{0}^{2\pi} \frac{1}{5 - 4\cos\theta} d\theta$$
