Q. P. Code: 38142



[Total Marks: 80]

N.B.: 1) Question No. 1 is Compulsory.

- 2) Answer any THREE questions from Q.2 to Q.6.
- 3) Figures to the right indicate full marks.
- Q.1 (a) Verify Cauchy-Schwartz inequality for u= (2, 1,-3) v= (3, 4,-2). (5)
 Also find angle between u & v.
 - (b) If $A = \begin{bmatrix} 2 & 0 & 0 \\ 5 & -1 & 0 \\ 2 & 3 & 3 \end{bmatrix}$ find Eigen values of $A^2 + 6A^{-1} 3I$. (5)
 - (c) Evaluate $\int_C \frac{z^3 + 2Z}{(Z-1)^2} dz$ when C is |z| = 2. (5)
 - (d) Find the extremals of $\int_{x_1}^{x_2} (x + y')y' dx$. (5)
- Q.2 (a) Verify Cayley-Hamilton theorem & hence find A^{-1} , where A = (6) $\begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & -1 \end{bmatrix}.$
 - (b) Find the extremal of $\int_{x_1}^{x_2} (2xy y''^2) dx$. (6)
 - (c) Obtain Laurent's series expansion of $f(z) = \frac{Z+2}{(Z-3)(Z-4)}$ about z=0.
- Q.3 (a) Evaluate $\int_0^{1+i} z^2 dz$ along the parabola $x = y^2$. (6)
 - (b) Show that $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$ is derogatory & find its minimal
 - (c) Reduce the following quadratic form into canonical form & (8) hence find it's rank, index, signature &value class $x^2 + 2y^2 + 3z^2 + 2yz + 2xy 2zx.$

- Q.4 (a) Find unit vector orthogonal to both u = (-6,4,2) v = (3,1,5).
 - (6)
 - (b) Evaluate $\int_{-\infty}^{\infty} \frac{x^2}{(x^2+1)(x^2+4)} dx.$ (c) Show that matrix $A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$ is diagonalizable. Also (8)find its diagonal and transforming matrix.
- Using Rayleigh-Ritz method find solution for the extremal of the (6) functional $\int_0^1 (2xy + y^2 - (y')^2) dx$ given y(0) = y(1) = 0.
 - (b) Find an orthonormal basis for the subspace of IR^3 using Gram-(6)Schmidt process where $s = \{(1,0,0), (3,7,-2), (0,4,1)\}$
 - (c) Find the curve C of given length 'l' which encloses a maximum (8)
- (6)If $A = \begin{bmatrix} \pi & \frac{\pi}{4} \\ 0 & \frac{\pi}{2} \end{bmatrix}$ find $\cos A$. Q.6 (a)
 - (b) Check whether the set of all pairs of real numbers of the form (6)(1, x) with operations
 - (1,a) + (1,b) = (1,a+b) and k(1,a) = (1,ka) is a vector space, where k is real number.
 - Find the singular value decomposition of $A = \begin{bmatrix} 2 & 3 \\ 0 & 2 \end{bmatrix}$. (8)