[Total Marks: 80

N.B.: (1) Question No. one is compulsory.

- (2) Answer any three questions from Q.2 to Q.6
- (3) Use of stastical Tables permitted.
- (4) Figures to the right indicate full marks
- 1. (a) Find the Eigen values of  $A^2 + 2I$ , where  $A = \begin{bmatrix} 1 & 0 & 0 \\ 2 & -2 & 0 \\ 3 & 5 & 3 \end{bmatrix}$  and I is the Identity matrix of order 2

(b) Evaluate the line integral  $\int_0^{1+i} (x^2 + iy) dz$  along the path y = x. If x is a continuous random variable x = x.

$$f(x) = \begin{cases} k(x - x^3) & 0 \le x \le 1 \\ 0 & otherwise \end{cases},$$

Find i) k ii) the mean of the distribution.

(d) Compute Spearman's rank correlation coefficient from the following data

X	18	20	34	52	12
Y	39	23	35	18	46

2. (a) Is the following matrix Derogatory? Justify.

$$\begin{bmatrix}
5 & -6 & -6 \\
-1 & 4 & 2 \\
3 & -6 & -4
\end{bmatrix}$$
(b) Evaluate  $\oint_C \frac{e^{2z}}{(z-1)^4} dz$  where c is the circle  $|z| = 2$ 

(c) The markscof 1000 students in an Examination are found to be normally distributed with mean 70 and standard deviation 5, estimate the number of students wkose marks will be i) between 60 and 75 ii) more than 75.

[Turn over

3. (a) Solve the following non-linear programming problem using Kuhn-Tucker conditions

Maximize 
$$z = 10x_1 + 4x_2 - 2x_1^2 - x_2^2$$

Subject to 
$$2x_1 + x_2 \le 5$$
; and  $x_1, x_2 \ge 0$ 

(b) Fit a Binomial distribution to the following data

x	0	1	2	3	4	5	6
F	5	18	28	12	7	6	4

(c) Is the following matrix diagonalizable? If yes, find the transforming matrix and the diagonal matrix.

$$\begin{bmatrix} 8 & -8 & -2 \\ 4 & -3 & -2 \\ 3 & -4 & 1 \end{bmatrix}$$

4. (a) Solve the following LPP using Simplex method

$$\begin{bmatrix} 8 & -8 & -2 \\ 4 & -3 & -2 \\ 3 & -4 & 1 \end{bmatrix}$$
we the following LPP using Simplex method
$$\text{Maximize } z = 4x_1 + x_2 + 3x_3 + 5x_4$$

$$\text{Subject to } -4x_1 + 6x_2 + 5x_3 + 4x_4 \ge 20$$

$$-3x_1 - 2x_2 + 4x_3 \Rightarrow x_4 \le 10$$

$$-8x_1 - 3x_2 + 3x_3 + 2x_4 \le 20$$

$$x_1, x_2, x_3, x_4 \ge 0$$
The random variable X follows the Poisson distribution such that

(b) If a random variable X follows the Poisson distribution such that

P(X = 1) = 2P(X = 2), find the mean, the variance of the distribution and

$$P(X=3)$$

(c) Expand  $f(z) = \frac{1}{z(z-2)(z+1)}$  in the regions

i)  $|z| \ll 1$ , ii) 1 < |z| < 2, iii) |z| > 2

i) 
$$|z| \iff 1$$
, ii)  $1 < |z| < 2$ , iii)  $|z| > 2$ 

[Turn over

6

- 5. (a) Evaluate using Cauchy's Residue theorem  $\oint_C \frac{2z-1}{z(2z+1)(z+2)} dz$  where c is |z| = 1.

  - (b) A certain stimulus administered to each of 12 patients resulted in the following change in blood pressure:

$$5, 2, 8, -1, 3, 0, -2, 1, 5, 0, 4, 6$$

Can it be concluded that the stimulus will increase the blood pressure (at 5%) level of significance.)?

(c) Solve the following LPP using the Dual Simplex method

Maximise 
$$z = -3x_1 - 2x_2$$

Subject to 
$$x_1 + x_2 \ge 1$$
  
$$x_1 + x_2 \le 7$$

$$x_1 + 2x_2 \ge 10$$

$$x_1 x_2 > 0$$

 $x_2 \le 3$   $x_1, x_2 \ge 0$  6.(a) Find the equations of lines of regression for the following data

x         5         6         7         8         9         10         11           v         11         14         14         15         12         17         16						Mintery		<u></u>
v 11 14 14 15 12 17 16	x	5	6	7	8	7.9	10	11
	y	11	14	14	(1.5	12	17	16

(c) Evaluate  $\int_{-\infty}^{\infty} \frac{x^2}{(x^2+1)(x^2+4)} dx$  using contour integration.

(b) In an experiments on pea breeding, the following frequencies of seeds were obtained

	Round and	Wrinkled and	Round and	Wrinkled	Total	
	Yellow	yellow	green	and green		
	315	101	108	32	556	
7	heory predicts	that the frequenc	ies should be in	proportions 9:	3: 3: 1.	
					· (11.	Tag4
.90	Examine the co	rrespondence bet	ween theory and	l experiment us	sing Chi-sq	uare Test 8
John Strain	Examine the co	rrespondence bet	ween theory and	l experiment us	sing Chi-sq	uare Test 8
J. bakes	Examine the co	rrespondence bet	ween theory and	experiment us	sing Chi-sq	uare Test 8