(46)

Q.P. Code :23022

[Time: Three Hours] | Marks:80|

Please check whether you have got the right question paper.

N.B: 1. Question.No.1 is compulsory.
2. Attempt any three questions from Q.2 to Q.6
3. Use of statistical table permitted.
4. Figures to the right indicate full marks.

Q.1 a) Evaluate $\int_C \log z \, dz$ where C is the unit circle in the z - plane. 05

b) Find the eigen values of the adjoint of $A = \begin{bmatrix} 2 & 0 & -1 \\ 0 & 2 & 0 \\ -1 & 0 & 2 \end{bmatrix}$ 05

c) If the arithmetic mean of regression coefficient is p and their difference is 2q, find the correlation coefficient. 05

d) Write the dual of the following L.P.P. 05
Maximise $Z = 2x_1 - x_2 + 4x_3$
Subject to $x_1 + 2x_2 - x_3 \leq 5$
$2x_1 - x_2 + x_3 \leq 6$
$x_1 + x_2 + 3x_3 \leq 10$
$4x_1 + x_3 \leq 12$
$x_1, x_2, x_3 \geq 0$

Q.2 a) Evaluate $\int_C \frac{\cot z}{z} \, dz$ where C is the ellipse $9x^2 + 4y^2 = 1$ 06

b) Show that $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{bmatrix}$ is non- derogatory. 06

c) If X is a normal variate with mean 10 and standard deviation 4, find 08
i)$P(|X - 14|<1)$, ii) $P(5 \leq X \leq 18)$, iii) $P(X \leq 12)$

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Q.3

a) Find the expectation of number of failures preceeding the first success in an infinite series 06
of independent trials with constant probabilities p & q of success and failure respectively.

b) Using Simplex Method solve the following L.P.P 06
Maximise $Z = 10x_1 + x_2 + x_3$
Subject to $\quad x_1 + x_2 - 3x_3 \leq 10$
$\qquad\qquad 4x_1 + x_2 + x_3 \leq 20$
$\qquad\qquad x_1, x_2, x_3 \geq 0$

c) Expand $f(z) = \dfrac{1}{z(z+1)(z-2)}$

(i) Within the unit circle about the origin. 08
(ii) with in the annulus region between the concentric circles about the origin having
radii 1 and 2 respectively.
(iii) In the exterior of the circle with centre at the origin and radius 2.

Q.4

a) If X is Binomial distributed with mean=2 and variance = 4/3, find the probability 06
distribution of X.

b) Calculate the value of rank correlation coefficient from the following data regarding score 06
of 6 students in physics & chemistry test.
Marks in Physics : 40, 42, 45, 35, 36, 39
Marks in Chemistry : 46, 43, 44, 39, 40, 43

c) Is the matrix A= $\begin{bmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$ diagonalisable? If so find the diagonal form and the 08
transforming matrix.

Q.5

a) A random sample of 50 items gives the mean 6.2 and standard deviation 10.24 . Can it be 06
regarded as drawn from a normal population with mean 5.4 at 5% level of significance?

b) Evaluate $\int_0^\infty \dfrac{dx}{(x^2+a^2)^3}$, a>0 Using Cauchy's residue theorem. 06

c) Using Kuhn-Tucker condition to solve the following N.L.P.P 08
Maximise $Z = 8x_1 + 10x_2 - x_1^2 - x_2^2$
Subject to $\quad 3x_1 + 2x_2 \leq 6$
$\qquad\qquad x_1, x_2 \geq 0$

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Q.6

a) The following table gives the number of accidents in a city during a week. Find whether   06
the accidents are uniformly distributed over a week.

Day:	Sun,	Mon,	Tue,	Wed,	Thu,	Fri,	Sat,	Total.
No. of accidents:	13	15	9	11	12	10	14	84

b) If two independent random samples of sizes 15 & 8 have respectively the following   06
means and population standard deviations,

$\overline{X_1} = 980$ $\qquad\qquad$ $\overline{X_2} = 1012$
$\sigma_1 = 75$ $\qquad\qquad$ $\sigma_2 = 80$

Test the hypothesis that $\mu_1 = \mu_2$ at 5% level of significance,

(Assume the population to be normal)

08

c) Using Penally (Big M) method solve the following L.P.P.
Minimise $Z = 2x_1 + x_2$
Subject to $\quad 3x_1 + x_2 = 3$
$\qquad\qquad 4x_1 + 3x_2 \geq 6$
$\qquad\qquad x_1 + 2x_2 \leq 3$
$\qquad\qquad x_1, x_2 \geq 0$

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