

3/03/2016



Signals & Systems 3 Hours)

[ Total Marks : 8 ]

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N.B.: (1) Question No.1 is compulsory.

- (2) Attempt any Three questions of the remaining questions.  
 (3) Assume suitable data wherever required.

1. (a) Check whether the following signals are periodic or not, if periodic, find the period.

$$(i) x(n) = e^{j\left(\frac{4\pi}{7}n + \frac{\pi}{3}\right)},$$

$$(ii) x(t) = e^{jn}$$

- (b) Check whether the system is linear or not, stable or not; where  $y(n)$  is the output,  $x(n)$  is the input of the system.

$$y(n) = (n + 1) e^{x(n)}.$$

- (c) Sketch the double side and single side spectrum of the signal

$$x(n) = 1 + \cos(6\pi n + \pi/3) + 8 \sin(8\pi n - \pi/3).$$

- (d) Find the Laplace transform of the signal

$$x(t) = e^{-2t}; \text{ specify ROC.}$$

- (e) Find the Z - transform of the signal

$$x(n) = 2^{-n} \cos\left(\frac{\pi n}{4}\right) u(n); \text{ specify ROC.}$$

2. (a) Let  $x(n) = u(n)$ ; check whether the signal is power signal or not, find the power and energy of the signal.

$$(b) x(t) = 3 - |t| \quad |t| \leq 3 \\ = 0 \quad \text{elsewhere}$$

Sketch (i)  $x(3 - t)$

(ii)  $x(3t + 2)$

(iii) Find energy of the signal  $x(t)$ .

- (c) Find the even and odd part of the signal

$$x(t) = u(t + 1) - u(t - 2).$$

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3. (a) Find the Linear convolution of the signal

$$\begin{aligned}x(t) &= 1 & |t| \leq 0.5 \\&= 0 & \text{elsewhere}\end{aligned}$$

$h(t) = u(t+1) - u(t-1)$ ; sketch the output signal.

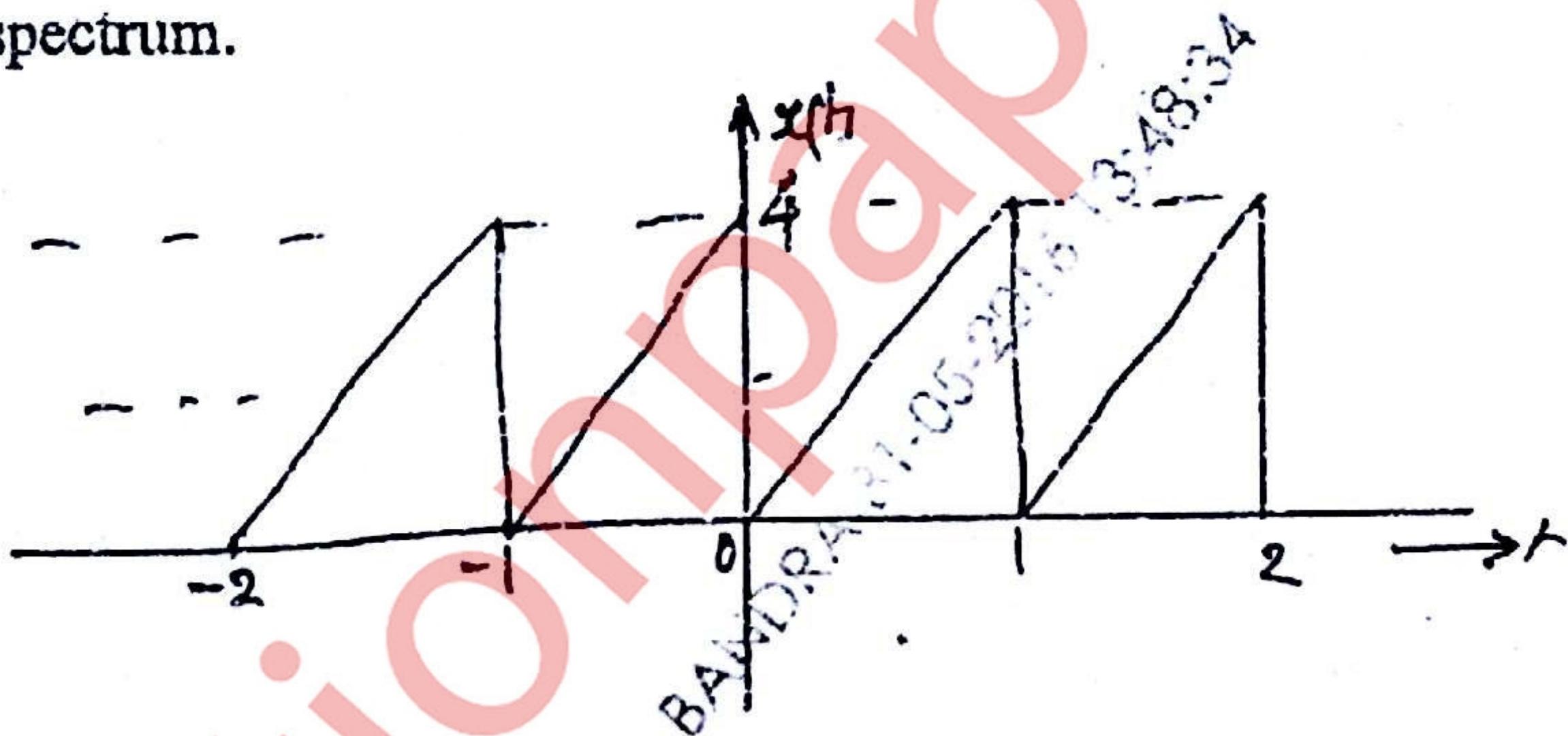
- (b) Find whether the system given by the impulse response is causal or not, stable or not.

$$h(n) = 2^{-n} u(n+1)$$

- (c) Find  $y(n) = x(n) * h(n)$  where

$$x(n) = [1, 2, 3, 4, -1, 6] \quad h(n) = [1, 2, -1, 2].$$

4. (a) Find the exponential Fourier series of the signal  $x(t)$  as given below. Sketch the spectrum.



- (b) Find DTFS of the signal

$$x(n) = \cos\left[\frac{\pi}{2}n\right]$$

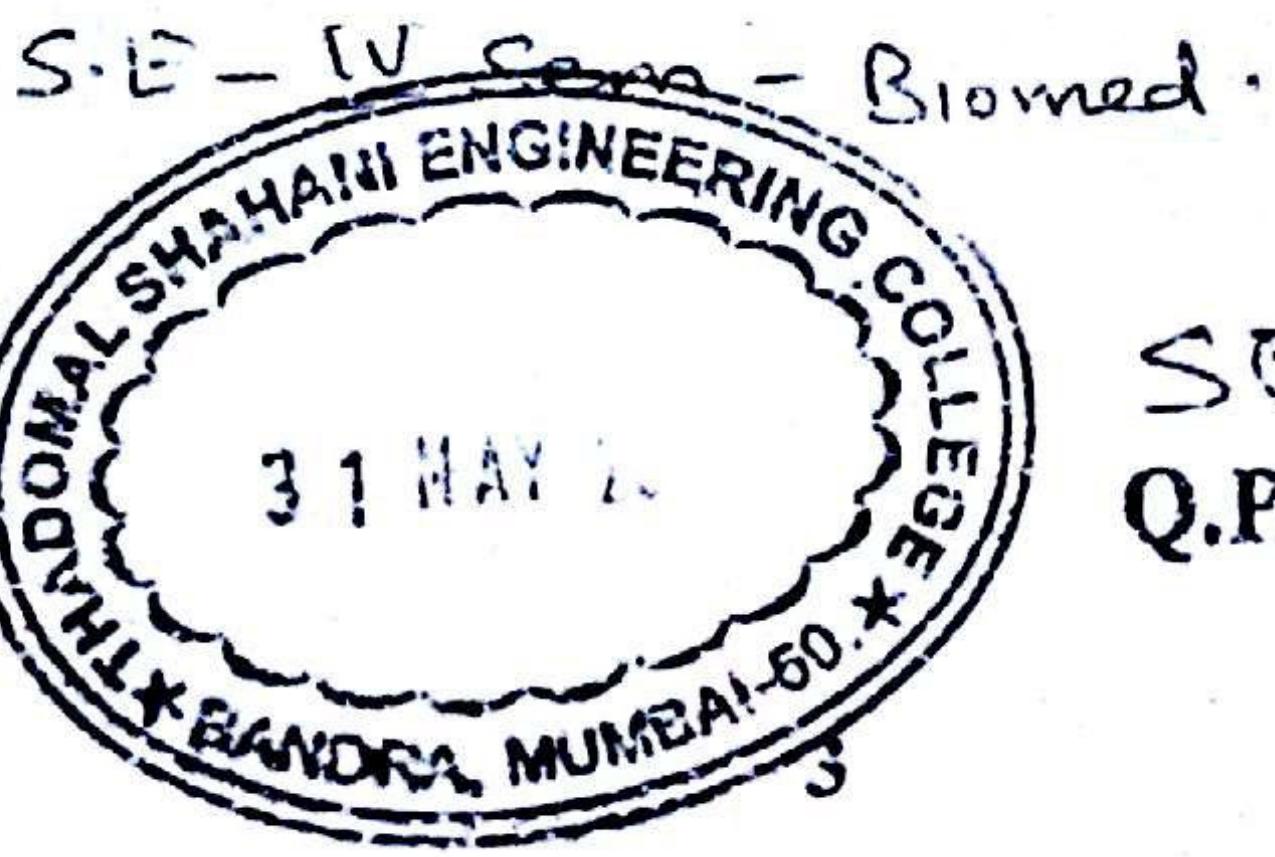
- (c) Find  $x(t)$  if  $X(\omega) = \frac{j\omega + 1}{(j\omega)^2 + 6j\omega + 8}$

5. (a) Find DTFT of the signal

$$x(n) = \left(\frac{1}{2}\right)^n u(n); \text{ Find magnitude and phase spectrum.}$$

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- (b) Prove the convolution property of Laplace transform. 6
- (c) Find  $h(t)$  if  $H(s) = \frac{s+5}{s^2(s+2)}$  if the system is causal. 8

6. (a) Find  $x(n)$  for all possible ROC if 10

$$x(z) = \frac{z^2(z - \gamma_2)}{(z - \gamma_3)(z - \frac{1}{3})(z - \gamma_4)}$$

- (b) Find the output of the system if  $x(n) = [1, 2, 3, -1, 2, -1, 2]$  and 6  
 $h[n] = [1, 0, -1, 1, 2]$  using linear convolution property of Z - transform.
- (c) Prove the time shifting property of Z - transform. 4