

Laplace's equation and find it corresponding analytic function

6. (a) Evaluate by Stoke's theorem  $\int_C (xydx + xy^2 dy)$  where C is the square in the xyplane with vertices (1,0), (0,1), (-1,0), and (0,-1)

(b) Find the bilinear transformation, which maps the points  $z = -1, 1, \infty$  onto the points w = -i, -1, i.

(c) Show that the general solution of  $\frac{d^2y}{dx^2} + 4x^2y = 0$  is  $y = \sqrt{x} \left[ A J_{1/4}(x^2) + B J_{-1/4}(x^2) \right]$  where A and B are constants.