

( 3 Hours )

[Total Marks : 80]

- N.B: 1. Solve any **FOUR** questions.  
 2. Assume suitable data if necessary and mention it clearly.  
 3. Draw sketches wherever required.  
 4. Use Annexure 1 and 2 for properties of water and air respectively.

- 1 (a) Define Grashof number? Physically what does Grashof number represents? How does Grashof number differ from Reynold's number? 5
- (b) A 12-cm-wide and 18-cm-high vertical hot surface in 30°C air is to be cooled by a heat sink with equally spaced fins of rectangular profile (Fig. 9-29). The fins are 0.1 cm thick and 18 cm long in the vertical direction and have a height of 2.4 cm from the base. Determine the optimum fin spacing and the rate of heat transfer by natural convection from the heat sink if the base temperature is 80°C. 10
- (c) Explain natural convection inside enclosures. 5
- 2 (a) 30 m long, 10 cm diameter hot water pipe of a district heating system is buried in the soil 50 cm below the ground surface. The outer surface temperature of the pipe is 80°C. Taking the surface temperature of the earth to be 10°C and the thermal conductivity of the soil at that location to be 0.9 W/m · °C, determine the rate of heat loss from the pipe. Take  $k = 0.9 \text{ W/m K}$ . 5
- (b) An ordinary egg can be approximated as a 5 cm diameter sphere. The egg is initially at a uniform temperature of 5°C and is dropped into boiling water at 95°C. Taking the convection heat transfer coefficient to be  $h = 1200 \text{ W/m}^2\text{K}$ , determine how long it will take for the center of the egg to reach 70°C. Take  $\lambda_l = 3.0754$ ,  $A_l = 1.9958$  5
- (c) What is conduction shape factor and how it is related to thermal resistance? 5
- (d) What do you mean by heat transfer in common configuration? Define conduction shape factor? 5
- 3 (a) The thermal contact conductance at the interface of two 1-cm-thick aluminum plates is measured to be 11,000 W/m<sup>2</sup> °C. Determine the thickness of the aluminum plate whose thermal resistance is equal to the thermal resistance of the interface between the plates. 5
- (b) How active and passive heat transfer enhancement techniques differ? 5
- (c) Explain how the thermal contact resistance can be minimized? 5
- (d) Consider a 2m high and 0.7m wide bronze plate whose thickness is 0.1 m. One side of the plate is maintained at a constant temperature of 600 K while the other side is maintained at 400 K. The thermal conductivity of the bronze plate can be assumed to vary linearly in that temperature range as  $k(T) = k_0(1+\beta T)$  where  $k_0 = 38 \text{ W/mK}$  and  $\beta = 9.21 \times 10^{-4} \text{ K}^{-1}$ . Disregarding the edge effects and assuming steady one-dimensional heat transfer, determine the rate of heat conduction through the plate. 5

- 4 (a) Water entering at  $10^{\circ}\text{C}$  is to be heated to  $40^{\circ}\text{C}$  in a tube of  $0.02\text{ m}$  inner diameter at a mass flow rate of  $0.01\text{ kg/s}$ . The outside of the tube is wrapped with an insulated electric heating element that produces a uniform flux of  $15\text{ kW/m}^2$  over the surface. Neglect entrance effect. Determine: (i) Reynolds number (ii) Heat transfer coefficient (iii) Length of pipe needed for a  $30^{\circ}\text{C}$  increase in average temperature (iv) Inner tube surface temperature at outlet (iv) Friction factor (v) Pressure drop in pipe. Pumping power required if pump is 50% efficient. 12
- (b) How heat transfer coefficient is enhanced in coiled tube? Define Dean Number. 4
- (c) Write the applications of laminar flow forced convection heat transfer. 4
- 5 (a) The condenser of a steam power plant operates at a pressure of  $7.38\text{ kPa}$ . Steam at this pressure condenses on the outer surfaces of horizontal pipes through which cooling water circulates. The outer diameter of the pipes is  $3\text{ cm}$ , and the outer surfaces of the pipes are maintained at  $30^{\circ}\text{C}$ . Determine (i) the rate of heat transfer to the cooling water circulating in the pipes and (ii) the rate of condensation of steam per unit length of a horizontal pipe. Use the properties of water in liquid and vapor state as per the Annexure – 1. 10
- (b) How does radiation transfer through a participating medium differ from that through a nonparticipating medium? 5
- (c) In condensate flow how wetted perimeter is defined? How it differs from ordinary perimeter? 5
- 6 (a) Consider a large uranium plate of thickness  $4\text{ cm}$  and thermal conductivity  $28\text{ W/m}^{\circ}\text{C}$  in which heat is generated uniformly at a constant rate of  $5 \times 10^6\text{ W/m}^3$ . One side of the plate is maintained at  $0^{\circ}\text{C}$  by iced water while the other side is subjected to convection to an environment at  $30^{\circ}\text{C}$  with a heat transfer coefficient of  $45\text{ W/m}^2{}^{\circ}\text{C}$ . Considering a total of three equally spaced nodes in the medium, two at the boundaries and one at the middle, estimate the exposed surface temperature of the plate under steady conditions using the finite difference approach. 10
- (b) Define these terms used in the finite difference formulation: node, nodal network, volume element, nodal spacing, and difference equation. 5
- (c) What are advantages and disadvantages of numerical and analytical methods? 5

## ANNEXURE - 1

## Properties of water

Temp. <i>T, °C</i>	Saturation Pressure <i>P<sub>sat</sub>, kPa</i>	Density <i>ρ, kg/m<sup>3</sup></i>		Enthalpy of Vaporization <i>h<sub>fg</sub>, kJ/kg</i>		Specific Heat <i>c<sub>p</sub>, J/kg·K</i>		Thermal Conductivity <i>k, W/m·K</i>		Dynamic Viscosity <i>μ, kg/m·s</i>		Prandtl Number <i>Pr</i>		Volume Expansion Coefficient <i>β, 1/K</i>
		Liquid	Vapor	Liquid	Vapor	Liquid	Vapor	Liquid	Vapor	Liquid	Vapor	Liquid	Vapor	Liquid
0.01	0.6113	999.8	0.0048	2501	4217	1854	0.561	0.0171	$1.792 \times 10^{-3}$	$0.922 \times 10^{-4}$	13.5	1.00	-0.068 × 10 <sup>-3</sup>	
5	0.8721	999.9	0.0068	2490	4205	1857	0.571	0.0173	$1.519 \times 10^{-3}$	$0.934 \times 10^{-4}$	11.2	1.00	0.015 × 10 <sup>-3</sup>	
10	1.2276	999.7	0.0094	2478	4194	1862	0.580	0.0176	$1.307 \times 10^{-3}$	$0.946 \times 10^{-4}$	9.45	1.00	0.733 × 10 <sup>-3</sup>	
15	1.7051	999.1	0.0128	2466	4185	1863	0.589	0.0179	$1.138 \times 10^{-3}$	$0.959 \times 10^{-4}$	8.09	1.00	0.138 × 10 <sup>-3</sup>	
20	2.339	998.0	0.0173	2454	4182	1867	0.598	0.0182	$1.002 \times 10^{-3}$	$0.973 \times 10^{-4}$	7.01	1.00	0.195 × 10 <sup>-3</sup>	
25	3.169	997.0	0.0231	2442	4180	1870	0.607	0.0186	$0.891 \times 10^{-3}$	$0.987 \times 10^{-4}$	6.14	1.00	0.247 × 10 <sup>-3</sup>	
30	4.246	996.0	0.0304	2431	4178	1875	0.615	0.0189	$0.798 \times 10^{-3}$	$1.001 \times 10^{-4}$	5.42	1.00	0.294 × 10 <sup>-3</sup>	
35	5.628	994.0	0.0397	2419	4178	1880	0.623	0.0192	$0.720 \times 10^{-3}$	$1.016 \times 10^{-4}$	4.83	1.00	0.337 × 10 <sup>-3</sup>	
40	7.384	992.1	0.0512	2407	4179	1885	0.631	0.0196	$0.653 \times 10^{-3}$	$1.031 \times 10^{-4}$	4.32	1.00	0.377 × 10 <sup>-3</sup>	
45	9.593	990.1	0.0655	2395	4180	1892	0.637	0.0200	$0.596 \times 10^{-3}$	$1.046 \times 10^{-4}$	3.91	1.00	0.415 × 10 <sup>-3</sup>	
50	12.35	988.1	0.0831	2383	4181	1900	0.644	0.0204	$0.547 \times 10^{-3}$	$1.062 \times 10^{-4}$	3.55	1.00	0.451 × 10 <sup>-3</sup>	
55	15.76	985.2	0.1045	2371	4183	1908	0.649	0.0208	$0.504 \times 10^{-3}$	$1.077 \times 10^{-4}$	3.25	1.00	0.484 × 10 <sup>-3</sup>	
60	19.94	983.3	0.1304	2359	4185	1916	0.654	0.0212	$0.467 \times 10^{-3}$	$1.093 \times 10^{-4}$	2.99	1.00	0.517 × 10 <sup>-3</sup>	
65	25.03	980.4	0.1614	2346	4187	1926	0.659	0.0216	$0.433 \times 10^{-3}$	$1.110 \times 10^{-4}$	2.75	1.00	0.548 × 10 <sup>-3</sup>	
70	31.19	977.5	0.1983	2334	4190	1936	0.663	0.0221	$0.404 \times 10^{-3}$	$1.126 \times 10^{-4}$	2.55	1.00	0.578 × 10 <sup>-3</sup>	
75	38.58	974.7	0.2421	2321	4193	1948	0.667	0.0225	$0.378 \times 10^{-3}$	$1.142 \times 10^{-4}$	2.38	1.00	0.607 × 10 <sup>-3</sup>	
80	47.39	971.8	0.2935	2309	4197	1962	0.670	0.0230	$0.355 \times 10^{-3}$	$1.159 \times 10^{-4}$	2.22	1.00	0.653 × 10 <sup>-3</sup>	
85	57.83	968.1	0.3536	2296	4201	1977	0.673	0.0235	$0.333 \times 10^{-3}$	$1.176 \times 10^{-4}$	2.08	1.00	0.670 × 10 <sup>-3</sup>	
90	70.14	965.3	0.4235	2283	4206	1993	0.675	0.0240	$0.315 \times 10^{-3}$	$1.193 \times 10^{-4}$	1.96	1.00	0.702 × 10 <sup>-3</sup>	
95	84.55	961.5	0.5045	2270	4212	2010	0.677	0.0246	$0.297 \times 10^{-3}$	$1.210 \times 10^{-4}$	1.85	1.00	0.716 × 10 <sup>-3</sup>	
100	101.33	957.9	0.5978	2257	4217	2029	0.679	0.0251	$0.282 \times 10^{-3}$	$1.227 \times 10^{-4}$	1.75	1.00	0.750 × 10 <sup>-3</sup>	
110	143.27	950.6	0.8263	2230	4229	2071	0.652	0.0262	$0.255 \times 10^{-3}$	$1.261 \times 10^{-4}$	1.58	1.00	0.798 × 10 <sup>-3</sup>	
120	198.53	943.4	1.121	2203	4244	2120	0.633	0.0275	$0.232 \times 10^{-3}$	$1.296 \times 10^{-4}$	1.44	1.00	0.858 × 10 <sup>-3</sup>	
130	270.1	934.6	1.496	2174	4263	2177	0.634	0.0288	$0.213 \times 10^{-3}$	$1.330 \times 10^{-4}$	1.33	1.01	0.913 × 10 <sup>-3</sup>	
140	361.3	921.7	1.965	2145	4286	2244	0.683	0.0301	$0.197 \times 10^{-3}$	$1.365 \times 10^{-4}$	1.24	1.02	0.970 × 10 <sup>-3</sup>	
150	475.8	916.6	2.546	2114	4311	2314	0.682	0.0316	$0.183 \times 10^{-3}$	$1.399 \times 10^{-4}$	1.16	1.02	1.025 × 10 <sup>-3</sup>	
160	617.8	907.4	3.256	2083	4340	2420	0.680	0.0331	$0.170 \times 10^{-3}$	$1.434 \times 10^{-4}$	1.09	1.05	1.145 × 10 <sup>-3</sup>	
170	791.7	897.7	4.119	2050	4370	2460	0.677	0.0347	$0.160 \times 10^{-3}$	$1.468 \times 10^{-4}$	1.03	1.05	1.178 × 10 <sup>-3</sup>	
180	1,002.1	887.3	5.153	2015	4410	2590	0.673	0.0364	$0.150 \times 10^{-3}$	$1.502 \times 10^{-4}$	0.983	1.07	1.210 × 10 <sup>-3</sup>	
190	1,254.4	876.4	6.388	1979	4460	2710	0.669	0.0382	$0.142 \times 10^{-3}$	$1.537 \times 10^{-4}$	0.947	1.09	1.280 × 10 <sup>-3</sup>	
200	1,553.8	864.3	7.852	1941	4500	2840	0.663	0.0401	$0.134 \times 10^{-3}$	$1.571 \times 10^{-4}$	0.910	1.11	1.350 × 10 <sup>-3</sup>	
220	2,318	840.3	11.60	1859	4610	3110	0.650	0.0442	$0.122 \times 10^{-3}$	$1.641 \times 10^{-4}$	0.865	1.15	1.520 × 10 <sup>-3</sup>	
240	3,344	813.7	16.73	1767	4760	3520	0.632	0.0487	$0.111 \times 10^{-3}$	$1.712 \times 10^{-4}$	0.836	1.24	1.720 × 10 <sup>-3</sup>	
260	4,688	783.7	23.69	1663	4970	4070	0.609	0.0540	$0.102 \times 10^{-3}$	$1.788 \times 10^{-4}$	0.832	1.35	2.000 × 10 <sup>-3</sup>	
280	6,412	750.8	33.15	1544	5280	4835	0.581	0.0605	$0.094 \times 10^{-3}$	$1.870 \times 10^{-4}$	0.854	1.49	2.380 × 10 <sup>-3</sup>	
300	8,581	713.8	46.15	1405	5750	5980	0.548	0.0695	$0.086 \times 10^{-3}$	$1.965 \times 10^{-4}$	0.902	1.69	2.950 × 10 <sup>-3</sup>	
320	11,274	667.1	64.57	1239	6540	7900	0.509	0.0836	$0.078 \times 10^{-3}$	$2.084 \times 10^{-4}$	1.00	1.97		
340	14,586	610.5	92.62	1028	8240	11,870	0.469	0.110	$0.070 \times 10^{-3}$	$2.255 \times 10^{-4}$	1.23	2.43		
360	18,651	528.3	144.0	720	14,690	25,800	0.427	0.178	$0.060 \times 10^{-3}$	$2.571 \times 10^{-4}$	2.06	3.73		
374.14	22,090	317.0	317.0	0	—	—	—	—	$0.043 \times 10^{-3}$	$4.313 \times 10^{-5}$				

## ANNEXURE - 2

## Properties of Air

Temp. <i>T, °C</i>	Density <i>ρ, kg/m³</i>	Specific Heat <i>c<sub>p</sub>, J/kg·K</i>	Thermal Conductivity <i>k, W/m·K</i>	Thermal Diffusivity <i>α, m²/s</i>	Dynamic Viscosity <i>μ, kg/m·s</i>	Kinematic Viscosity <i>ν, m²/s</i>	Prandtl Number <i>Pr</i>
-150	2.866	983	0.01171	$4.158 \times 10^{-6}$	$8.636 \times 10^{-6}$	$3.013 \times 10^{-6}$	0.7246
-100	2.038	966	0.01582	$8.036 \times 10^{-6}$	$1.189 \times 10^{-5}$	$5.837 \times 10^{-6}$	0.7263
-50	1.582	999	0.01979	$1.252 \times 10^{-5}$	$1.474 \times 10^{-5}$	$9.319 \times 10^{-6}$	0.7440
-40	1.514	1002	0.02057	$1.356 \times 10^{-5}$	$1.527 \times 10^{-5}$	$1.008 \times 10^{-5}$	0.7436
-30	1.451	1004	0.02134	$1.465 \times 10^{-5}$	$1.579 \times 10^{-5}$	$1.087 \times 10^{-5}$	0.7425
-20	1.394	1005	0.02211	$1.578 \times 10^{-5}$	$1.630 \times 10^{-5}$	$1.169 \times 10^{-5}$	0.7408
-10	1.341	1006	0.02288	$1.696 \times 10^{-5}$	$1.680 \times 10^{-5}$	$1.252 \times 10^{-5}$	0.7387
0	1.292	1006	0.02364	$1.818 \times 10^{-5}$	$1.729 \times 10^{-5}$	$1.338 \times 10^{-5}$	0.7362
5	1.269	1006	0.02401	$1.880 \times 10^{-5}$	$1.754 \times 10^{-5}$	$1.382 \times 10^{-5}$	0.7350
10	1.246	1006	0.02439	$1.944 \times 10^{-5}$	$1.778 \times 10^{-5}$	$1.426 \times 10^{-5}$	0.7336
15	1.225	1007	0.02476	$2.009 \times 10^{-5}$	$1.802 \times 10^{-5}$	$1.470 \times 10^{-5}$	0.7323
20	1.204	1007	0.02514	$2.074 \times 10^{-5}$	$1.825 \times 10^{-5}$	$1.516 \times 10^{-5}$	0.7309
25	1.184	1007	0.02551	$2.141 \times 10^{-5}$	$1.849 \times 10^{-5}$	$1.562 \times 10^{-5}$	0.7296
30	1.164	1007	0.02588	$2.208 \times 10^{-5}$	$1.872 \times 10^{-5}$	$1.608 \times 10^{-5}$	0.7282
35	1.145	1007	0.02625	$2.277 \times 10^{-5}$	$1.895 \times 10^{-5}$	$1.655 \times 10^{-5}$	0.7268
40	1.127	1007	0.02662	$2.346 \times 10^{-5}$	$1.918 \times 10^{-5}$	$1.702 \times 10^{-5}$	0.7255
45	1.109	1007	0.02699	$2.416 \times 10^{-5}$	$1.941 \times 10^{-5}$	$1.750 \times 10^{-5}$	0.7241
50	1.092	1007	0.02735	$2.487 \times 10^{-5}$	$1.963 \times 10^{-5}$	$1.798 \times 10^{-5}$	0.7228
60	1.059	1007	0.02808	$2.632 \times 10^{-5}$	$2.008 \times 10^{-5}$	$1.896 \times 10^{-5}$	0.7202
70	1.028	1007	0.02881	$2.780 \times 10^{-5}$	$2.052 \times 10^{-5}$	$1.995 \times 10^{-5}$	0.7177
80	0.9994	1008	0.02953	$2.931 \times 10^{-5}$	$2.096 \times 10^{-5}$	$2.097 \times 10^{-5}$	0.7154
90	0.9718	1008	0.03024	$3.085 \times 10^{-5}$	$2.139 \times 10^{-5}$	$2.201 \times 10^{-5}$	0.7132
100	0.9458	1009	0.03095	$3.243 \times 10^{-5}$	$2.181 \times 10^{-5}$	$2.306 \times 10^{-5}$	0.7111
120	0.8977	1011	0.03235	$3.565 \times 10^{-5}$	$2.264 \times 10^{-5}$	$2.522 \times 10^{-5}$	0.7073
140	0.8542	1013	0.03374	$3.898 \times 10^{-5}$	$2.345 \times 10^{-5}$	$2.745 \times 10^{-5}$	0.7041
160	0.8148	1016	0.03511	$4.241 \times 10^{-5}$	$2.420 \times 10^{-5}$	$2.975 \times 10^{-5}$	0.7014
180	0.7788	1019	0.03646	$4.593 \times 10^{-5}$	$2.504 \times 10^{-5}$	$3.212 \times 10^{-5}$	0.6992
200	0.7459	1023	0.03779	$4.954 \times 10^{-5}$	$2.577 \times 10^{-5}$	$3.455 \times 10^{-5}$	0.6974
250	0.6746	1033	0.04104	$5.890 \times 10^{-5}$	$2.760 \times 10^{-5}$	$4.091 \times 10^{-5}$	0.6946
300	0.6158	1044	0.04418	$6.871 \times 10^{-5}$	$2.934 \times 10^{-5}$	$4.765 \times 10^{-5}$	0.6935
350	0.5664	1056	0.04721	$7.892 \times 10^{-5}$	$3.101 \times 10^{-5}$	$5.475 \times 10^{-5}$	0.6937
400	0.5243	1069	0.05015	$8.951 \times 10^{-5}$	$3.261 \times 10^{-5}$	$6.219 \times 10^{-5}$	0.6948
450	0.4880	1081	0.05298	$1.004 \times 10^{-4}$	$3.415 \times 10^{-5}$	$6.997 \times 10^{-5}$	0.6965
500	0.4565	1093	0.05572	$1.117 \times 10^{-4}$	$3.563 \times 10^{-5}$	$7.806 \times 10^{-5}$	0.6986
600	0.4042	1115	0.06093	$1.352 \times 10^{-4}$	$3.846 \times 10^{-5}$	$9.515 \times 10^{-5}$	0.7037
700	0.3627	1135	0.06581	$1.598 \times 10^{-4}$	$4.111 \times 10^{-5}$	$1.133 \times 10^{-4}$	0.7092
800	0.3289	1153	0.07037	$1.855 \times 10^{-4}$	$4.362 \times 10^{-5}$	$1.326 \times 10^{-4}$	0.7149
900	0.3008	1169	0.07465	$2.122 \times 10^{-4}$	$4.600 \times 10^{-5}$	$1.529 \times 10^{-4}$	0.7206
1000	0.2772	1184	0.07868	$2.398 \times 10^{-4}$	$4.826 \times 10^{-5}$	$1.741 \times 10^{-4}$	0.7260
1500	0.1990	1234	0.09599	$3.908 \times 10^{-4}$	$5.817 \times 10^{-5}$	$2.922 \times 10^{-4}$	0.7478
2000	0.1553	1264	0.11113	$5.664 \times 10^{-4}$	$6.630 \times 10^{-5}$	$4.270 \times 10^{-4}$	0.7539